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Sandia National Laboratories
Waste Isolation Pilot Plant

**Thermodynamic Model for the Na-B(OH)₃-Cl-SO₄
system, Revision 1, Superseding ERMS 55811**

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YX/10/30/12

Work Carried Out under Task 10 of AP-155: Analysis Plan for Thermodynamic Properties
Including Pitzer Parameters for Solubility Studies of Borate.
To be included in the AP-155 records package

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1 INTRODUCTION

This analysis report (AR) provides the results of derivation of thermodynamic properties including Pitzer parameters based on solubility of sodium tetraborate (borax) in NaCl and Na₂SO₄ solutions. Sodium tetraborate and borax are used interchangeably in this AR.

The computer code EQ3/6 Version 8.0a (Wolery, 2008; Wolery et al., 2010; Xiong, 2011) was used for this analysis. Wolery (2008), Wolery et al. (2010) and Xiong (2011b) completed the qualification of Version 8.0a of EQ3/6 according to Sandia National Laboratories' (SNL's) WIPP quality assurance (QA) procedures for WIPP compliance-related actinide solubility calculations, and US EPA approved it on September 27, 2011.

This analysis was carried out under Task 10 of AP-155 (Xiong, 2011c). There are two deviations from AP-155. The first deviation is that the literature data from Sborgi et al. (1924) and Reardon (1976) are also used for derivation of thermodynamic parameters, in addition to experimental data produced at SNL Carlsbad Facility. The second deviation is that the Python script developed by Kirchner (2012) is used instead of the one developed by Nemer (2010).

Table 1 (see next page) defines the generic abbreviations, acronyms, and initialisms used in this report and other analysis reports.

The author recently found out that the EQ6 output files for comparison of the model developed in this work with the literature data were produced by using the database, data0.pdl, without incorporation of the parameters generated in this work. In this revision, the EQ6 output files have been reproduced by using the data0.pdl in which the parameters determined in this study have been incorporated, and the affected table is updated.

Table 1. Abbreviations, Acronyms, and Initialisms.

Abbreviation, Acronym, or Initialism	Definition
acetate	CH_3COO^- or CH_3CO_2^-
Am, Am(III)	americium, americium in the +III oxidation state
am	amorphous
anhydrite	CaSO_4
AP	analysis plan
aq	aqueous
aragonite	CaCO_3 , a polymorph of CaCO_3 that is metastable with respect to calcite
atm	atmosphere(s)
B, B(III)	boron, boron in the +III oxidation state
Br, Br(-I)	bromine, bromine in the -I oxidation state
brucite	$\text{Mg}(\text{OH})_2$
C	carbon
Ca, Ca(II), Ca^{2+}	calcium, calcium in the +II oxidation state, calcium ion
calcite	CaCO_3 , the thermodynamically stable polymorph of CaCO_3
citrate	$(\text{CH}_2\text{COO})_2\text{C}(\text{OH})(\text{COO})^{3-}$ or $(\text{CH}_2\text{CO}_2)_2\text{C}(\text{OH})(\text{CO}_2)^{3-}$
Cl, Cl(-I), Cl^-	chlorine, chlorine in the -I oxidation state, chloride ion
CMS	(Sandia/WIPP software) Configuration Management System
CO_2	carbon dioxide
CO_3^{2-}	carbonate
CRA-2009	the second WIPP Compliance Recertification Application, submitted to the EPA in March 2009
DB	(thermodynamic) database
DOE	(U.S.) Department of Energy
dolomite	$\text{CaMg}(\text{CO}_3)_2$, a carbonate mineral that is nucleates and grows slowly under low-temperature conditions and is often suppressed (prevented from forming) in geochemical modeling calculations
DRZ	disturbed rock zone
EDTA	ethylenediaminetetraacetate, $(\text{CH}_2\text{COO})_2\text{N}(\text{CH}_2)_2\text{N}(\text{CH}_2\text{COO})_2^{4-}$ or $(\text{CH}_2\text{CO}_2)_2\text{N}(\text{CH}_2)_2\text{N}(\text{CH}_2\text{CO}_2)^{4-}$
EPA	(U.S.) Environmental Protection Agency
EQ3/6	a geochemical software package for speciation and solubility calculations (EQ3NR) and reaction-path calculations (EQ6)

Table 1 continued on next page

Table 1. Abbreviations, Acronyms, and Initialisms (continued).

Abbreviation, Acronym, or Initialism	Definition
ERDA-6	Energy Research and Development Administration (WIPP Well) 6, a synthetic brine representative of fluids in Castile brine reservoirs
f_{CO_2}	fugacity (similar to the partial pressure) of CO_2
Fm.	Formation
FMT	Fracture-Matrix Transport, a geochemical speciation and solubility code
GWB	Generic Weep Brine, a synthetic brine representative of intergranular Salado brines at or near the stratigraphic horizon of the repository
gypsum	$\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$
H or H_2 , H^+	hydrogen or hydrogen ion
halite	NaCl
H_2O	water (aq, g, or contained in solid phases)
hydromagnesite	$\text{Mg}_5(\text{CO}_3)_4(\text{OH})_2 \cdot 4\text{H}_2\text{O}$
I	ionic strength
K, K(I)	potassium, potassium in the +I oxidation state
kg	kilogram(s)
M	molar
m	meter(s) or molal
magnesite	MgCO_3
Mg, Mg(II)	magnesium, magnesium in the +II oxidation state
MgO	magnesium oxide, used to refer to the WIPP engineered barrier, which includes periclase as the primary constituent and various impurities
mM	millimolar
Na, Na(I), Na^+	sodium, sodium in the +I oxidation state, sodium ion
nesquehonite	$\text{MgCO}_3 \cdot 3\text{H}_2\text{O}$
Np, Np(V)	neptunium, neptunium in the +V oxidation state
O or O_2	oxygen
OH, OH^-	hydroxide or hydroxide ion
oxalate	$(\text{COO})^{2-}$ or $\text{C}_2\text{O}_4^{2-}$
PA	performance assessment
PABC	Performance Assessment Baseline Calculations

Table 1 continued on next page

Table 1. Abbreviations, Acronyms, and Initialisms (continued).

Abbreviation, Acronym, or Initialism	Definition
periclase	pure, crystalline MgO, the primary constituent of the WIPP engineered barrier
pH	the negative, common logarithm of the activity of H ⁺
pcH	the negative, common logarithm of the molar concentration of H ⁺
phase 3	Mg ₂ Cl(OH) ₃ ·4H ₂ O
phase 5	Mg ₃ (OH) ₅ Cl·4H ₂ O
polyhalite	K ₂ MgCa ₂ (SO ₄) ₄ ·2H ₂ O
QA	quality assurance
Rev.	revision
RH	relative humidity
S, S(VI), SO ₄ ²⁻	sulfur, sulfur in the +VI oxidation state, sulfate ion
s	solid
SCA	S. Cohen and Associates
SNL	Sandia National Laboratories
Th, Th(IV)	thorium, thorium in the +IV oxidation state
TIC	total inorganic C
WIPP	(U.S. DOE) Waste Isolation Pilot Plant
wt %	weight percent
μ ⁰ /RT	dimensionless standard chemical potential

2 METHODS

The objective of this analysis was to derive thermodynamic properties in the Na^+ – $\text{B}(\text{OH})_3$ – Cl^- – SO_4^{2-} system based on solubility data of sodium tetraborate in NaCl solutions produced at SNL (Xiong, 2012a) and in Na_2SO_4 solutions from the literature (Sborgi et al., 1924). Table 2 lists experimental data in NaCl solutions from Xiong (2012a), and Table 3 lists experimental data in Na_2SO_4 solutions from Sborgi et al. (1924).

Felmy and Weare (1986) developed a thermodynamic model concerning borate in the system Na–K–Ca–Mg–H–Cl– SO_4 – CO_2 – $\text{B}(\text{OH})_4$ – H_2O , based on literature data. This model will be abbreviated as the FW86 model hereafter. Their model is an extension of the Harvie et al. (1984) model to include borate species. In the FW86 model, the species, $\text{NaB}(\text{OH})_4(\text{aq})$, was not explicitly considered. However, numerous researchers have suggested the existence of this complex in solutions containing sodium (e.g., Reardon, 1976; Corti et al., 1980; Rowe et al., 1989; Pokrowski et al., 1995; Akinfiev et al., 2006). Therefore, this complex could be important in Na-rich solutions.

In the work of Reardon (1976), the formation constants for the reaction,

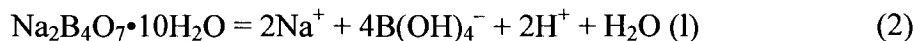


were determined in NaCl solutions with ionic strengths ranging from 0.165 m to 0.499 m at temperatures from 10 °C to 50 °C. To obtain the thermodynamic formation constants at infinite dilution, Reardon (1976) used the activity coefficients of HCO_3^- and $\text{H}_3\text{BO}_3(\text{aq})$ to approximate those of $\text{B}(\text{OH})_4^-$ and $\text{NaB}(\text{OH})_4(\text{aq})$, respectively. The thermodynamic formation constant at 25 °C for Reaction (1) obtained by Reardon (1976) was 0.22 ± 0.10 .

In this study, conditional formation constants for Reaction (1) generated by Reardon (1976) are re-evaluated by using the specific ion interaction theory (SIT) model, following the methodology of Grenthe et al. (1992). The $\log \beta_1$ at 25 °C obtained is 0.25 ± 0.01 (Figure 1 and Table 4). Based on $\Delta\epsilon = -0.04 \pm 0.02$, the $\log \beta_1$ at 10 °C, 40 °C and 50 °C are also obtained (Table 4). These values are in agreement with those of Pokrowski et al. (1995). The spreadsheet for calculation of these parameters is named XIONG_NaB(OH)4(aq)_SIT.xls and is located in the zip file Task10_DataPackage_Borate.zip.

The above $\log \beta_1$ for $\text{NaB}(\text{OH})_4(\text{aq})$, the experimental solubility data for borax in NaCl gathered under TP 10-01 and reported the milestone report (Xiong, 2012a), and solubility data of borax in Na_2SO_4 from Sborgi et al. (1924), are utilized to derive the Pitzer parameters and $\log K_{sp}$ for borax with the aid of the computer code EQ3/6 Version 8.0a (Wolery et al., 2010; Xiong,

2011b). The essence of the modeling is to minimize the difference between experimental and model predicted values. The $\log K_{sp}$ for borax dissolution refers to the following reaction,



Using experimental solubility data of sodium tetraborate for NaCl solutions (Xiong, 2012a), $\log K_{sp}$ for sodium tetraborate and $\lambda_{\text{Na}^+-\text{NaB}(\text{OH})_4(\text{aq})}$ are obtained. The values for these two parameters are evaluated by using the Python script (Na2B4O7_NaCl_Brute_PSD.py) which runs the EQ3CodeModule optimization routine (Kirchner, 2012) with EQ3NR input files NaTC-1.3i through NaTC-85.3i. These files are located in the folder labeled as “EQ3_NaCl” in the zip file “Task10_DataPackage_Borate.zip”. The optimization results indicate that the residual is minimized to be 0.26 when $\log K_{sp}$ is -24.80 and $\lambda_{\text{Na}^+-\text{NaB}(\text{OH})_4(\text{aq})}$ is between 0.093-0.098 (see Results_Na2B4O7_NaCl_Brute_PSD.txt, which is located in the folder named as “EQ3_NaCl”). An uncertainty of ± 0.10 is assigned to $\log K_{sp}$, and of 0.005 is assigned to $\lambda_{\text{Na}^+-\text{NaB}(\text{OH})_4(\text{aq})}$. The EQ3CodeModule optimization routine has been independently validated (Xiong, 2012b). The provisional database for the modeling is data0.psd, which is the precursor of data0.pd1 (see comment lines in data0.pd1 in Domski, 2012).

The experimental data of sodium tetraborate from Sborgi et al. (1924) (Table 3) are used to evaluate Ψ_{ijk} for the interaction of $\text{SO}_4^{-2}-\text{B}_4\text{O}_5(\text{OH})_4^{-2}-\text{Na}^+$. In the evaluation, θ_{ij} for $\text{B}(\text{OH})_4^- - \text{SO}_4^{-2}$ was set to 0.17 ± 0.03 , similar to the values for $\text{B}_3\text{O}_3(\text{OH})_4^- - \text{SO}_4^{-2}$ and $\text{B}_4\text{O}_5(\text{OH})_4^{2-} - \text{SO}_4^{-2}$ (Felmy and Weare, 1986). The Ψ_{ijk} for the interaction of $\text{SO}_4^{-2}-\text{B}_4\text{O}_5(\text{OH})_4^{-2}-\text{Na}^+$ is evaluated as 0.1 ± 0.2 using the Python script (Na2B4O7_Na2SO4_BRUTE_OneParameter_data0psd.py) with EQ3NR input files SO4-1.3i through SO4-7.3i. These input files are located in the folder labeled as “EQ3_Na2SO4” in the zip file “Task10_DataPackage_Borate.zip”. The value selected for the Ψ_{ijk} parameter is 0.1 ± 0.2 with a residual of 0.14-0.19 (see Results_Na2B4O7_Na2SO4_Brute_PSD.txt, which is located in the folder “EQ3_Na2SO4”).

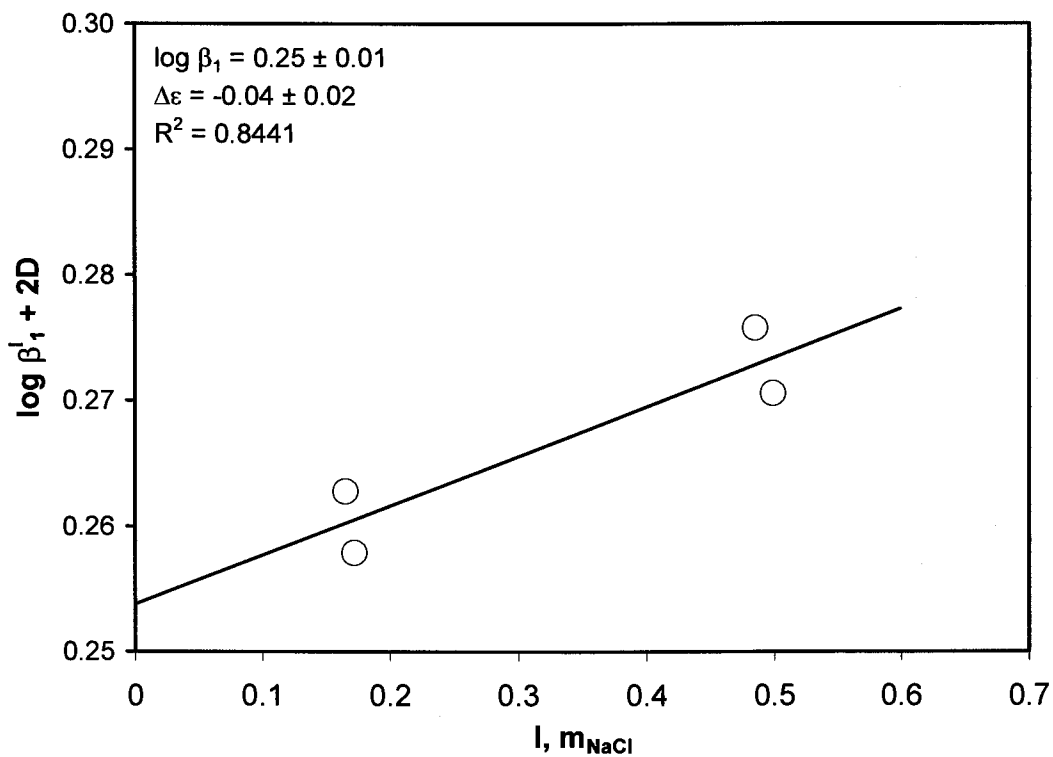


Figure 1. A plot showing $[\log \beta_1' + 2D]$ as a function of ionic strengths, where $\log \beta_1'$ denotes conditional formation constants of $\text{NaB}(\text{OH})_4(\text{aq})$ at certain ionic strengths from Reardon (1976).

Table 2. Experimental results concerning solubility of sodium tetraborate in NaCl solutions produced at SNL at 22.5 ± 1.5 °C (from Xiong, 2012a)*.

Experimental Number	Supporting Medium, NaCl, Experimental molal	Experimental time, days	pmH**	Molal solubility of sodium tetraborate expressed as total boron concentrations, $m_{\Sigma B}$
Na ₂ B ₄ O ₇ -NaCl-0.01-1	0.010	132	9.10	0.515
Na ₂ B ₄ O ₇ -NaCl-0.01-2	0.010	132	9.03	0.509
Na ₂ B ₄ O ₇ -NaCl-0.1-1	0.10	132	8.97	0.435
Na ₂ B ₄ O ₇ -NaCl-0.1-2	0.10	132	8.95	0.417
Na ₂ B ₄ O ₇ -NaCl-1.0-1	1.0	132	8.70	0.179
Na ₂ B ₄ O ₇ -NaCl-1.0-2	1.0	132	8.72	0.194
Na ₂ B ₄ O ₇ -NaCl-2.0-1	2.1	132	8.66	0.157
Na ₂ B ₄ O ₇ -NaCl-2.0-2	2.1	132	8.81	0.147
Na ₂ B ₄ O ₇ -NaCl-3.0-1	3.2	132	8.81	0.139
Na ₂ B ₄ O ₇ -NaCl-3.0-2	3.2	132	8.77	0.143
Na ₂ B ₄ O ₇ -NaCl-4.0-1	4.4	132	8.88	0.165
Na ₂ B ₄ O ₇ -NaCl-4.0-2	4.4	132	8.89	0.151
Na ₂ B ₄ O ₇ -NaCl-5.0-1	5.0	132	8.80	0.145
Na ₂ B ₄ O ₇ -NaCl-5.0-2	5.0	132	8.79	0.146
Na ₂ B ₄ O ₇ -NaCl-0.01-1	0.010	278	9.28	0.488
Na ₂ B ₄ O ₇ -NaCl-0.01-2	0.010	278	9.28	0.495
Na ₂ B ₄ O ₇ -NaCl-0.1-1	0.10	278	9.26	0.411
Na ₂ B ₄ O ₇ -NaCl-0.1-2	0.10	278	9.24	0.415
Na ₂ B ₄ O ₇ -NaCl-1.0-1	1.0	278	9.04	0.190
Na ₂ B ₄ O ₇ -NaCl-1.0-2	1.0	278	9.03	0.099
Na ₂ B ₄ O ₇ -NaCl-2.0-1	2.1	278	9.00	0.155
Na ₂ B ₄ O ₇ -NaCl-2.0-2	2.1	278	8.98	0.152
Na ₂ B ₄ O ₇ -NaCl-3.0-1	3.2	278	8.96	0.143
Na ₂ B ₄ O ₇ -NaCl-3.0-2	3.2	278	8.93	0.140
Na ₂ B ₄ O ₇ -NaCl-4.0-1	4.4	278	9.06	0.139
Na ₂ B ₄ O ₇ -NaCl-4.0-2	4.4	278	9.05	0.142
Na ₂ B ₄ O ₇ -NaCl-5.0-1	5.0	278	8.96	0.141
Na ₂ B ₄ O ₇ -NaCl-5.0-2	5.0	278	8.96	0.142
Na ₂ B ₄ O ₇ -NaCl-0.01-1	0.010	327	9.33	0.482
Na ₂ B ₄ O ₇ -NaCl-0.01-2	0.010	327	9.28	0.508
Na ₂ B ₄ O ₇ -NaCl-0.1-1	0.10	327	9.26	0.436

Na ₂ B ₄ O ₇ -NaCl-0.1-2	0.10	327	9.22	0.430
Na ₂ B ₄ O ₇ -NaCl-1.0-1	1.0	327	9.09	0.207
Na ₂ B ₄ O ₇ -NaCl-1.0-2	1.0	327	9.10	0.210
Na ₂ B ₄ O ₇ -NaCl-2.0-1	2.1	327	8.99	0.160
Na ₂ B ₄ O ₇ -NaCl-2.0-2	2.1	327	9.00	0.161
Na ₂ B ₄ O ₇ -NaCl-3.0-1	3.2	327	9.00	0.151
Na ₂ B ₄ O ₇ -NaCl-3.0-2	3.2	327	8.95	0.157
Na ₂ B ₄ O ₇ -NaCl-4.0-1	4.4	327	9.10	0.151
Na ₂ B ₄ O ₇ -NaCl-4.0-2	4.4	327	9.11	0.147
Na ₂ B ₄ O ₇ -NaCl-5.0-1	5.0	327	8.97	0.151
Na ₂ B ₄ O ₇ -NaCl-5.0-2	5.0	327	9.01	0.158
Na ₂ B ₄ O ₇ -NaCl-0.01-1	0.010	377	9.39	0.513
Na ₂ B ₄ O ₇ -NaCl-0.01-2	0.010	377	9.38	0.509
Na ₂ B ₄ O ₇ -NaCl-0.1-1	0.10	377	9.32	0.468
Na ₂ B ₄ O ₇ -NaCl-0.1-2	0.10	377	9.33	0.482
Na ₂ B ₄ O ₇ -NaCl-1.0-1	1.0	377	9.09	0.214
Na ₂ B ₄ O ₇ -NaCl-1.0-2	1.0	377	9.09	0.231
Na ₂ B ₄ O ₇ -NaCl-2.0-1	2.1	377	9.03	0.168
Na ₂ B ₄ O ₇ -NaCl-2.0-2	2.1	377	9.03	0.171
Na ₂ B ₄ O ₇ -NaCl-3.0-1	3.2	377	9.01	0.153
Na ₂ B ₄ O ₇ -NaCl-3.0-2	3.2	377	9.00	0.149
Na ₂ B ₄ O ₇ -NaCl-4.0-1	4.4	377	9.08	0.152
Na ₂ B ₄ O ₇ -NaCl-4.0-2	4.4	377	9.09	0.146
Na ₂ B ₄ O ₇ -NaCl-5.0-1	5.0	377	9.00	0.152
Na ₂ B ₄ O ₇ -NaCl-5.0-2	5.0	377	9.02	0.149
Na ₂ B ₄ O ₇ -NaCl-0.01-1	0.010	425	9.35	0.514
Na ₂ B ₄ O ₇ -NaCl-0.01-2	0.010	425	9.31	0.532
Na ₂ B ₄ O ₇ -NaCl-0.1-1	0.10	425	9.26	0.531
Na ₂ B ₄ O ₇ -NaCl-0.1-2	0.10	425	9.25	0.458
Na ₂ B ₄ O ₇ -NaCl-1.0-1	1.0	425	9.04	0.221
Na ₂ B ₄ O ₇ -NaCl-1.0-2	1.0	425	9.03	0.222
Na ₂ B ₄ O ₇ -NaCl-2.0-1	2.1	425	8.96	0.171
Na ₂ B ₄ O ₇ -NaCl-2.0-2	2.1	425	8.97	0.171
Na ₂ B ₄ O ₇ -NaCl-3.0-1	3.2	425	8.95	0.161
Na ₂ B ₄ O ₇ -NaCl-3.0-2	3.2	425	8.93	0.156
Na ₂ B ₄ O ₇ -NaCl-4.0-1	4.4	425	9.02	0.158
Na ₂ B ₄ O ₇ -NaCl-4.0-2	4.4	425	9.04	0.154
Na ₂ B ₄ O ₇ -NaCl-5.0-1	5.0	425	8.96	0.159

Na ₂ B ₄ O ₇ -NaCl-5.0-2	5.0	425	8.97	0.162
Na ₂ B ₄ O ₇ -NaCl-0.01-1	0.010	567	9.28	0.489
Na ₂ B ₄ O ₇ -NaCl-0.01-2	0.010	567	9.28	0.497
Na ₂ B ₄ O ₇ -NaCl-0.1-1	0.10	567	9.24	0.429
Na ₂ B ₄ O ₇ -NaCl-0.1-2	0.10	567	9.23	0.426
Na ₂ B ₄ O ₇ -NaCl-1.0-1	1.0	567	9.00	0.199
Na ₂ B ₄ O ₇ -NaCl-1.0-2	1.0	567	9.00	0.203
Na ₂ B ₄ O ₇ -NaCl-2.0-1	2.1	567	8.94	0.157
Na ₂ B ₄ O ₇ -NaCl-2.0-2	2.1	567	8.94	0.167
Na ₂ B ₄ O ₇ -NaCl-3.0-1	3.2	567	8.93	0.160
Na ₂ B ₄ O ₇ -NaCl-3.0-1R	3.2	567	8.92	0.155
Na ₂ B ₄ O ₇ -NaCl-3.0-2	3.2	567	8.90	0.154
Na ₂ B ₄ O ₇ -NaCl-4.0-1	4.4	567	8.99	0.148
Na ₂ B ₄ O ₇ -NaCl-4.0-2	4.4	567	9.01	0.152
Na ₂ B ₄ O ₇ -NaCl-5.0-1	5.0	567	8.93	0.158
Na ₂ B ₄ O ₇ -NaCl-5.0-2	5.0	567	8.93	0.154

*Experimental data at 567 days were not reported in Xiong (2012a). They were generated after that report (see Pages 10–11 of WIPP–Borate–5).

**In Xiong (2012a), pH reading were reported. Values of pmH reported in this analysis report are calculated by using the correction factors (A_M) for pH readings, and conversion factors (Θ) from molarity to molality, $\text{pmH} = \text{pH}_{\text{ob}} + A_M - \log \Theta$ (Xiong et al., 2010). The correction factors are from Rai et al. (1995). The conversion factors are calculated from densities for NaCl solutions, which are from Söhnel and Novotný (1985). Please see the spreadsheet “XIONG_Na2B4O7_NaCl_Paper.xls”.

Table 3. Solubility data of sodium tetraborate in Na₂SO₄ solutions at 25 °C (Sborgi et al., 1924).

Molal solubility of sodium tetraborate expressed as total boron concentrations, $m_{\Sigma B}$	Molality of SO ₄ ²⁻	Molality of Na ⁺
0.3344*	0.0000*	0.1672*
0.2868	0.08711	0.3176
0.2281	0.2393	0.5927
0.1699	0.7633	1.6115
0.1585	1.036	2.151
0.1576	1.318	2.715
0.1573	1.439	2.956
0.1572	1.503	3.085

*These data were not used for calculation, because there was no SO₄²⁻ in solution.

Table 4. Equilibrium Constants for Complex Formation Reaction

Reaction	log β_l at 25 °C unless otherwise noted
$\text{Na}^+ + \text{B}(\text{OH})_4^- = \text{NaB}(\text{OH})_4(\text{aq})$	0.29 ± 0.01 (10 °C) 0.25 ± 0.01 (25 °C) with $\Delta\varepsilon = -0.04 \pm 0.02$ 0.24 ± 0.01 (40 °C) 0.26 ± 0.02 (50 °C)

Table 5. Locations of the Excel Spreadsheets, EQ3/6 I/O Files Associated with Calculations for This Analysis.

Description or Title of File(s)	Location of File(s)
Spreadsheet XIONG_NaB(OH)4(aq)_SIT.xls	In zip file Task10_DataPackage_Borate.zip, library LIBAP155
Spreadsheet XIONG_Na2B4O7_NaCl_Paper.xls	In zip file Task10_DataPackage_Borate.zip, library LIBAP155
EQ3/6 DB DATA0.PSD EQ3/6 DB DATA0.PD1	In zip file Task10_DataPackage_Borate.zip, library LIBAP155
EQ3/6 I/O files: NaTC-1.3i/o through NaTC-85.3i/o SO4-1.3i/o through SO4-7.3i/o ClSO4-1.3i/o through ClSO4-8.3i/o ClSO4-1.6i/o through ClSO4-8.6i/o	In zip file Task10_DataPackage_Borate.zip, library LIBAP155
Python scripts: Na2B4O7_NaCl_BRUTE_PSD.py Na2B4O7_Na2SO4_BRUTE_OneParameter_data0psd.py	In zip file Task10_DataPackage_Borate.zip, library LIBAP155
EQ3/6 DB DATA0.PD1 containing the parameters obtained in this work	In zip file Task10_AR_Rev1_DataPKG.zip, library LIBAP155
EQ3/6 I/O files: ClSO4-1.6i/o through ClSO4-8.6i/o; produced by using DATA0.PD1 containing the parameters obtained in this work	In zip file Task10_AR_Rev1_DataPKG.zip, library LIBAP155

The EQ3/6 thermodynamic databases (DB) DATA0.FM1 and DATA0.PSD were used for this analysis. The DATA0.FM1 (Xiong, 2001a) has the Felmy and Weare (1986) model on

borate species. The DATA0.PSD database contains the revised parameters for the borate species generated in this analysis. The DATA0.PSD database is in Task10_DataPackage_Borate.zip, LIBAP155, in the CMS. All supporting EQ3/6 input and output (I/O) files are also located in the above zip file.

3 RESULTS

Table 6 provides the Pitzer parameters and $\log K_{sp}$ derived in this study.

Table 7 provides the comparison between the FW86 model and the revised model developed in this study. These two models are benchmarked versus the independent experimental data. The comparison demonstrates that the model developed in this study is superior in prediction of solubilities of sodium tetraborate in concentrated brines to ionic strengths of ~ 8 m. The EQ3/6 input and output files for the model comparison are CISO4-1.3i/o through CISO4-8.3i/o, and CISO4-1.6i/o through CISO4-8.6i/o, respectively. In the folder labeled as “Felmy” in the zip file “Task10_DataPackage_Borate.zip”, output files were generated by using the officially released database, data0.fm1 (Xiong, 2011a). In the folder labeled as “Xiong_Yongliang” in the zip file “Task10_DataPackage_Borate.zip”, output files were generated by using the provisional database, DATA0.PD1 (Domski, 2012), in which the data0.fm1 has been modified by incorporating the respective parameters described in this report. As data0.fm1 has been officially released, it is not included in the zip file.

Table 6. The revised thermodynamic model for the Na–B(OH)₃–Cl–SO₄ system developed in this study*.

Pitzer Mixing Parameters and Interaction Parameters Involving Neutral Species				
Species, <i>i</i>	Species, <i>j</i>	Species, <i>k</i>	θ_{ij} or λ_{ij}	Ψ_{ijk} or ζ_{ijk}
B(OH) ₄ ⁻	SO ₄ ⁻²		0.17 ± 0.03	
NaB(OH) ₄ (aq)	Na ⁺		0.093 ± 0.005	
B ₄ O ₅ (OH) ₄ ⁻²	SO ₄ ⁻²	Na ⁺		0.1 ± 0.2
Equilibrium Constants for Solubility and Complex Formation Reactions				
Reaction			log <i>K</i> or log β _l at 25 °C unless otherwise noted	
Na ₂ B ₄ O ₇ •10H ₂ O = 2Na ⁺ + 4B(OH) ₄ ⁻ + 2H ⁺ + H ₂ O			-24.80 ± 0.10 (2σ)	
Na ⁺ + B(OH) ₄ ⁻ = NaB(OH) ₄ (aq)			0.25 ± 0.01 (25 °C)	

*Unless otherwise noted, other parameters, which are not listed, are the same as those in Felmy and Weare (1986) model.

Table 7. Comparison of independent, experimental equilibrium compositions for multiple equilibrium assemblages containing sodium tetraborate ($\text{Na}_2\text{B}_4\text{O}_7 \cdot 10\text{H}_2\text{O}$) (borax) with predicted compositions in mixtures of NaCl and Na_2SO_4 at 25 °C*

Experimental data for equilibrium compositions					
m_{Na}	m_{Cl}	m_{SO_4}	$m_{\Sigma\text{B}}$	Equilibrium Assemblage**	References
6.967	5.516	0.694	0.125	BRX+HLT+THNDT	Van't Hoff and Blasdale (1905)
6.355	5.925	0.183	0.128	BRX+HLT	Grushvitski and Flerinskava (1932)
6.527	5.408	0.526	0.134	BRX+HLT	<i>ibid.</i>
6.716	5.286	0.673	0.167	BRX+HLT	<i>ibid.</i>
6.939	5.441	0.716	0.132	BRX+HLT+THNDT	<i>ibid.</i>
6.603	4.723	0.903	0.149	BRX	<i>ibid.</i>
6.477	3.168	1.619	0.141	BRX+MRBLT+THNDT	<i>ibid.</i>
3.774	0.248	1.734	0.117	BRX+MRBLT	<i>ibid.</i>
Equilibrium compositions predicted by the Felmy and Weare (1986) model, produced by using data0.fm1					
m_{Na}	m_{Cl}	m_{SO_4}	$m_{\Sigma\text{B}}$	Equilibrium Assemblage**	
6.971	5.484	0.691	0.212	BRX+HLT+THNDT	
6.364	5.896	0.182	0.206	BRX+HLT	
6.532	5.381	0.523	0.209	BRX+HLT	
6.704	5.260	0.670	0.211	BRX+HLT	
6.943	5.413	0.712	0.212	BRX+HLT+THNDT	
6.602	4.699	0.898	0.214	BRX	
6.367	3.229	1.512	0.229	BRX+MRBLT+THNDT	
3.833	0.246	1.721	0.289	BRX+MRBLT	
Equilibrium compositions predicted by the model developed in this study, produced by using data0.pd1					
m_{Na}	m_{Cl}	m_{SO_4}	$m_{\Sigma\text{B}}$	Equilibrium Assemblage**	
6.947	5.494	0.692	0.136	BRX+HLT+THNDT	
6.347	5.906	0.183	0.151	BRX+HLT	
6.512	5.393	0.524	0.141	BRX+HLT	
6.683	5.272	0.671	0.137	BRX+HLT	
6.922	5.426	0.714	0.136	BRX+HLT+THNDT	
6.577	4.711	0.900	0.131	BRX	
6.284	3.273	1.475	0.120	BRX+MRBLT+THNDT	

3.780	0.247	1.728	0.151	BRX+MRBLT
Difference in %** between experimental values and those predicted by the FW86 model				
ΔNa in %	ΔCl in %	ΔSO_4 in %	$\Delta\Sigma\text{B}$ in %	Equilibrium Assemblage**
0.060	-0.586	-0.507	69.788	BRX+HLT+THNDT
0.133	-0.483	-0.482	60.851	BRX+HLT
0.084	-0.496	-0.497	55.925	BRX+HLT
-0.170	-0.504	-0.503	26.362	BRX+HLT
0.072	-0.508	-0.507	60.305	BRX+HLT+THNDT
-0.016	-0.514	-0.515	43.776	BRX
-1.701	1.941	-6.656	62.343	BRX+MRBLT+THNDT
1.555	-0.725	-0.725	145.848	BRX+MRBLT
Difference in %*** between experimental values and those predicted by the model developed in this study				
ΔNa in %	ΔCl in %	ΔSO_4 in %	$\Delta\Sigma\text{B}$ in %	Equilibrium Assemblage**
-0.290	-0.402	-0.274	9.240	BRX+HLT+THNDT
-0.121	-0.309	-0.308	18.448	BRX+HLT
-0.227	-0.284	-0.285	5.249	BRX+HLT
-0.495	-0.275	-0.274	-18.006	BRX+HLT
-0.245	-0.273	-0.272	2.587	BRX+HLT+THNDT
-0.392	-0.259	-0.260	-11.967	BRX
-2.974	3.327	-8.884	-14.637	BRX+MRBLT+THNDT
0.145	-0.307	-0.307	28.758	BRX+MRBLT

*Comparison was performed by running EQ3/6 calculations. In EQ3NR calculations, input compositions for total Na^+ , total Cl^- , and total SO_4^{2-} are the same as the experimental values, and for total $\text{B}(\text{OH})_4^-$ is at trace level (1×10^{-20} m). In EQ6 calculations, the above compositions are in equilibrium with sodium tetraborate (borax), and a new set of compositions for total Na^+ , total Cl^- , total SO_4^{2-} , and total $\text{B}(\text{OH})_4^-$ is obtained.

**Abbreviations for minerals: BRX, borax ($\text{Na}_2\text{B}_4\text{O}_7 \cdot 10\text{H}_2\text{O}$); HLT, halite (NaCl); MRBLT, mirabilite ($\text{Na}_2\text{SO}_4 \cdot 10\text{H}_2\text{O}$); THNDT, thenardite (Na_2SO_4).

***Difference in % is defined as, using concentrations of sodium on molal scale as an example,

$$\Delta\text{Na in \%} = 100 \times \frac{m_{\text{Na,Model}} - m_{\text{Na,Experimental}}}{m_{\text{Na,Experimental}}}$$

4 CONCLUSIONS

In this analysis report, a thermodynamic model with high precision is developed for the $\text{Na}^+ - \text{B}(\text{OH})_3 - \text{Cl}^- - \text{SO}_4^{2-}$ system, based on new experimental data. This model is validated by independent experimental data in ternary mixtures of NaCl and Na_2SO_4 . With this model, solubilities of borax in concentrated NaCl, Na_2SO_4 , and NaCl+ Na_2SO_4 solutions can be accurately modeled.

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